

MATHEMATICS LABORATORY ACTIVITY

Class X | CBSE Curriculum

Chapter 2: Polynomials

1. Topic

To verify geometrically the number of zeroes of a quadratic polynomial $p(x) = ax^2 + bx + c$ by drawing its graph and observing its intersection with the X-axis.

2. Objective

To understand that:

- A quadratic polynomial can have 0, 1, or 2 real zeroes.
- The zeroes of a polynomial $p(x)$ are the x-coordinates of the points where the graph of $y = p(x)$ intersects the X-axis.
- This can be verified by plotting the polynomial on graph paper and observing how many times the parabola crosses or touches the X-axis.

3. Pre-Requisite Knowledge

- Concept of a polynomial and degree of a polynomial.
- Meaning of zeroes of a polynomial: A zero of a polynomial $p(x)$ is a value of x for which $p(x) = 0$.
- Standard form of a quadratic polynomial: $p(x) = ax^2 + bx + c$, where $a \neq 0$.
- Knowledge of the Cartesian coordinate system — X-axis, Y-axis, and plotting ordered pairs (x, y) .
- Concept of a parabola and how the direction (opening up/down) depends on the sign of 'a'.
- If $a > 0$, the parabola opens upward; if $a < 0$, the parabola opens downward.

4. Materials Required

- Graph paper (squared, 1 cm ruled)
- Sharp pencil, eraser, and ruler (30 cm scale)
- Coloured pens or sketch pens (red, blue, green) for drawing curves
- Geometry box (compass and set squares)
- Scientific calculator (optional, for verification)
- A thick cardboard or drawing board to fix the graph paper

5. Procedure

Follow the steps given below for each of the three cases:

Case 1: $p(x) = x^2 + 2$ (Upward Parabola — No Real Zeroes)

Step 1: Prepare a table of values by substituting integer values of x from -4 to 4 .

$$x = -4, -3, -2, -1, 0, 1, 2, 3, 4$$

$$y = 18, 11, 6, 3, 2, 3, 6, 11, 18$$

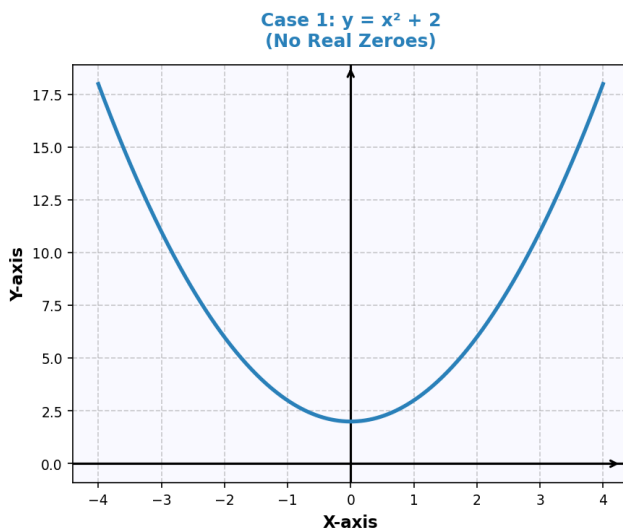
Step 2: Draw the X-axis and Y-axis on the graph paper. Choose a suitable scale (1 cm = 1 unit on X-axis; 1 cm = 2 units on Y-axis).

Step 3: Plot the ordered pairs (x, y) obtained in Step 1 on the graph paper.

Step 4: Join all the plotted points with a smooth free-hand curve (parabola) using a blue pen.

Step 5: Observe whether the parabola intersects the X-axis. The parabola lies entirely ABOVE the X-axis and does NOT cross it.

→ **Conclusion:** The parabola does not intersect the X-axis, hence $p(x) = x^2 + 2$ has NO real zeroes.



Case 2: $p(x) = x^2$ (Upward Parabola — One Zero at Origin)

Step 1: Prepare a table of values:

$$x = -4, -3, -2, -1, 0, 1, 2, 3, 4$$

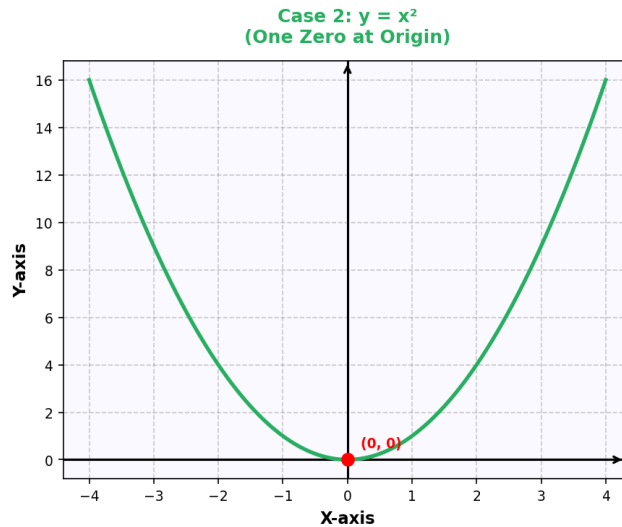
$$y = 16, 9, 4, 1, 0, 1, 4, 9, 16$$

Step 2: Draw the axes and choose a suitable scale (1 cm = 1 unit on X-axis; 1 cm = 2 units on Y-axis).

Step 3: Plot the points on graph paper and join them with a smooth curve using a green pen.

Step 4: Observe the parabola. It just TOUCHES the X-axis at the origin (0, 0) and does not cross it.

→ **Conclusion:** The parabola touches the X-axis at exactly one point (0, 0), so $x = 0$ is the only zero of $p(x) = x^2$.



Case 3: $p(x) = -x^2 + 4$ (Downward Parabola — Two Distinct Zeroes)

Step 1: Prepare a table of values:

$$x = -4, -3, -2, -1, 0, 1, 2, 3, 4$$

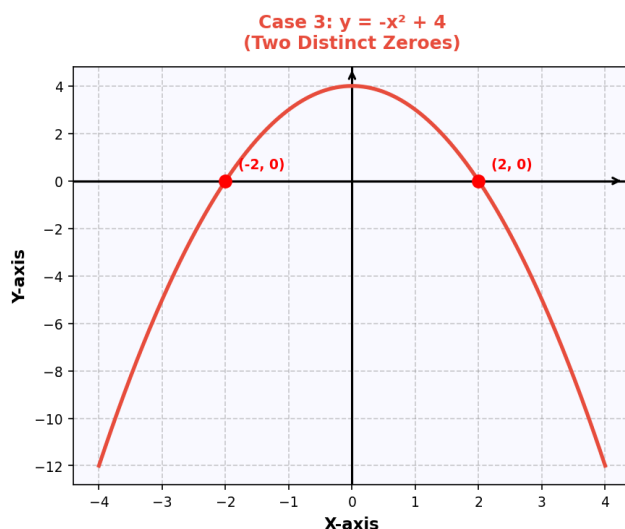
$$y = -12, -5, 0, 3, 4, 3, 0, -5, -12$$

Step 2: Draw the axes on graph paper. Choose scale: 1 cm = 1 unit on both axes.

Step 3: Plot all the ordered pairs and join them with a smooth downward-opening curve using a red pen.

Step 4: Mark the two points where the parabola crosses the X-axis: $(-2, 0)$ and $(2, 0)$ using a red dot.

→ **Conclusion:** The parabola cuts the X-axis at two distinct points $(-2, 0)$ and $(2, 0)$, so $x = -2$ and $x = 2$ are the two zeroes of $p(x) = -x^2 + 4$.



6. Observation

After plotting the three quadratic polynomials on graph paper, the following observations were made:

Case	Polynomial	Nature of Parabola	Number of Zeroes	Co-ordinates of Zero(es)
Case 1	$p(x) = x^2 + 2$	Upward Parabola (No X-axis intersection)	0 (No Zeroes)	None
Case 2	$p(x) = x^2$	Upward Parabola (Touches X-axis at origin)	1 (One Zero)	(0, 0)
Case 3	$p(x) = -x^2 + 4$	Downward Parabola (Cuts X-axis at two pts)	2 (Two Zeroes)	(-2, 0) and (2, 0)

Key Observations:

- In Case 1, the parabola $y = x^2 + 2$ opens upward and its vertex is at (0, 2), which lies above the X-axis. It does not intersect the X-axis at any point. Hence, the polynomial has no real zeroes.
- In Case 2, the parabola $y = x^2$ opens upward and its vertex is exactly at the origin (0, 0), which lies ON the X-axis. It touches the X-axis at exactly one point. Hence, $x = 0$ is the only (repeated) zero.
- In Case 3, the parabola $y = -x^2 + 4$ opens downward (since $a = -1 < 0$). It cuts the X-axis at two distinct points: (-2, 0) and (2, 0). Hence, $x = -2$ and $x = 2$ are two distinct real zeroes.

7. Result

It is verified geometrically that a quadratic polynomial $p(x) = ax^2 + bx + c$ can have:

1. **NO real zeroes** — when the parabola does not intersect the X-axis at all (e.g., $p(x) = x^2 + 2$). This happens when the discriminant $b^2 - 4ac < 0$.
2. **EXACTLY ONE real zero** — when the parabola just touches the X-axis at one point (e.g., $p(x) = x^2$). This happens when the discriminant $b^2 - 4ac = 0$.
3. **TWO distinct real zeroes** — when the parabola cuts the X-axis at two different points (e.g., $p(x) = -x^2 + 4$). This happens when the discriminant $b^2 - 4ac > 0$.

Thus, the number of zeroes of a quadratic polynomial is equal to the number of times its graph (parabola) intersects or touches the X-axis.

★★★ End of Activity ★★★